

# E) Solving One-Step Inequalities

**Solution Set** = All of the values of the variable that make the inequality true.

## Inequality Symbols

$$1 > -2$$

$$3 < 5$$

$$X \geq 3$$

$$X \leq 4$$

Read as "1 is **greater than** 2"

Read as "3 is **less than** 5"

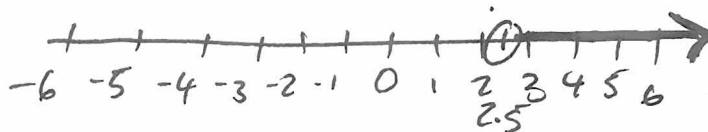
Read as "X is **greater than or equal to** 3"

Read as "X is **less than or equal to** 4"

Solve the inequality. Graph your solution.

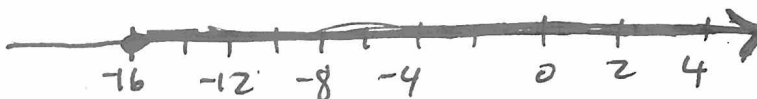
1)  $x - 6 > -3.5$

$$\begin{array}{r} +6 \quad +6 \\ \hline x > 2.5 \end{array}$$



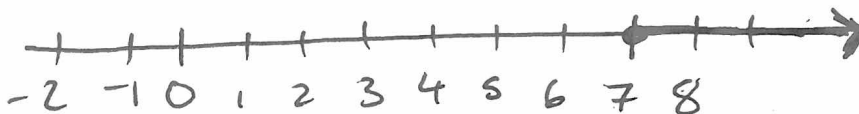
2)  $-8 \leq 8 + y$

$$\begin{array}{r} -8 \quad -8 \\ \hline -16 \leq y \\ y \geq -16 \end{array}$$



3)  $-1\frac{1}{3} \leq p - 8\frac{1}{3}$

$$\begin{array}{r} +8\frac{1}{3} \quad +8\frac{1}{3} \\ \hline 7 \leq p \\ p \geq 7 \end{array}$$



4)  $\frac{x}{4} < 5$

$$\begin{array}{r} (4) \frac{x}{4} < 5(4) \\ x < 20 \end{array}$$



5)  $-6x < 18$

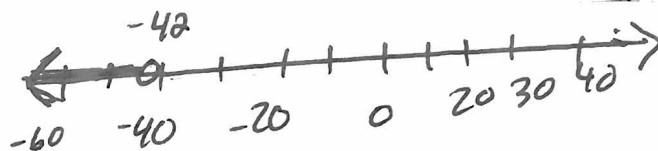
$$\begin{array}{r} -6 \quad -6 \\ \hline x > -3 \end{array}$$



$$6) \frac{x}{-6} > 7$$

$$(-6) \left( \frac{x}{-6} \right) > 7(-6)$$

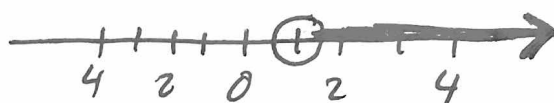
$$x < -42$$



F) Solving Multi-Step Inequalities  
Solve the inequality. Then Graph.

$$1) -7x + 2 < -5$$

$$\begin{array}{r} -2 \quad -2 \\ \hline -7x < -7 \\ \hline -7 \quad -7 \\ \hline x < 1 \end{array}$$



$$2) \frac{1}{3}(3x + 6) \geq -1$$

$$(3) \frac{1}{3}(3x + 6) \geq -1(3)$$

$$\begin{array}{r} 3x + 6 \geq -3 \\ -6 \quad -6 \\ \hline 3x \geq -9 \end{array}$$

$$\frac{3x}{3} \geq \frac{-9}{3} \quad x \geq -3$$



$$3) 14x + 5 < 7(2x - 3)$$

$$\begin{array}{r} 14x + 5 < 14x - 21 \\ -14x \quad -14x \\ \hline 5 < -21 \end{array}$$

$$5 < -21$$

False No Solution

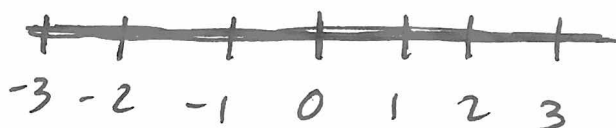


$$4) 12x - 1 > 6(2x - 1)$$

$$\begin{array}{r} 12x - 1 > 12x - 6 \\ -12x \quad -12x \\ \hline -1 > -6 \end{array}$$

$$-1 > -6$$

True



All real numbers!

Final Notes:

- Dividing or Multiplying by a negative flips the inequality sign
- $\leq$  and  $\geq$  are closed circles on the number line
- $<$  and  $>$  are open circles on the number line
- Untrue or false inequalities are no solution
- True ~~without~~ 1 variables inequalities are all real numbers